## Math 101 Final Exam Spring 2022

Make sure that your scantron matches the color of this page. **Read** <u>ALL</u> **directions carefully before beginning the exam**.

- Anyone found using a graphing/programmable calculator or cell phone during the final exam will receive a grade of "0".
- You may write on this exam. You may not use other paper unless you raise your hand and it is provided by an instructor.
- If you finish after 45 minutes, you can take this test with you. If you finish prior to 45 minutes, you will need to turn this test in along with your scantron.
- Please turn in your scantron to <u>YOUR</u> teaching assistant and have a picture ID ready.
- On your scantron, encode your name as specified on the scantron, encode your Dawgtag as your "Identification Number," and encode your **Section** # "OP" under the area labeled "Special Codes."

# SAMPLE SCANTRON

LAST	) PHN	ηĒ	/	- 5	P	A (	Ē	_	F	7(	25	T	N	Ar	n	E			,
$\begin{array}{c} \mathbf{A} \\ $											000000000000000000000000000000000000000	0000 20 20 2000		0000 S B1 00000 NU S S					
MO. Jan. () Feb. () Mar. () Apr. () Jun. () Jul. () Aug. () Sep. ()		0000000		R. 01234500		□ □ 0 0 0 0 0 0 0 0 0 0 0 0 0				000000000000000000000000000000000000000				00000000000000000000000000000000000000		000000000000000000000000000000000000000		00000000000000000000000000000000000000	

# **INSTRUCTOR/DAYS IS GIVEN:**

Section #	Days	Time	Instructor
02	WF	9-9:50	Daniel Davidson
03	WF	10-10:50	An Q Tran
04	TR	10-10:50	Ryan A Steele
05	TR	11-11:50	Sunil Kumar Lal Karn
11	TR	1-1:50	Gabriel E Ngwe
12	WF	1-1:50	Vina M Castelli

1. If you are given odds of 5 to 9 in favor of winning a bet, what is the probability of winning the bet?

(A) None of these	(B) <sup>5</sup> / <sub>9</sub>	$(C)\frac{5}{14}$	(D) $\frac{4}{9}$	(E) $\frac{4}{5}$
-------------------	---------------------------------	-------------------	-------------------	-------------------

**2.** A number is randomly drawn from the following set: {1, 2, 3, 4, 5, 6, 7, 8}. What is the probability that the number is greater than 8?

(A) None of these (B)  $\frac{7}{8}$  (C)  $\frac{3}{4}$  (D)  $\frac{5}{8}$  (E)  $\frac{1}{2}$ 

3.

Use Kruskal's algorithm to find the minimum spanning tree for the weighted graph. Give the total weight of the minimum spanning tree.



**4.** A store has an item listed for \$670.00. On Saturday they are having a 25% off sale where they give a 25% discount to all items in the store. What is the sale price of this item on Saturday? Round appropriately.

(A) None of these (B) \$167.50 (C) \$645.00 (D) \$335.00 (E) \$502.50

- **5.** The table shows the distribution, by age and gender, 30.8 million people who live alone in a certain region. Use the data in the table to find the probability that a randomly selected person living alone in the region is in the 25-34 age range.
  - (A) 0.08

(B) 0.14		Ages	Ages	Ages	Ages	Ages	Ages	<b>T</b> . 1
(C) 0.18		18-24	20-34	33-44	43-64	65-14	≥75	lotal
(c) 0.10	Male	0.8	2.4	2.9	4.5	1.5	1.2	13.3
(D) 0.57	Female	0.9	1.9	1.8	5.0	2.8	5.1	17.5
(E) None of these	Total	1.7	4.3	4.7	9.5	4.3	6.3	30.8

6. Suppose your credit card has a balance of \$8,700 and an annual interest rate of 14%. You decide to pay off the balance over three years. If there are no further purchases charged to the card, (i) How much must you pay each month? (round to the nearest dollar)(ii) How much total interest will you pay?

(A) (i) \$309	(B) (i) \$309	(C) (i) \$297	(D) (i) \$297
(ii) \$2,424	(ii) \$816	(ii) \$672	(ii) \$1,992

7. A data representation that is constructed by separating each data item into two parts

based on place value is called a \_\_\_\_\_.

- A) Histogram
- B) Probability distribution
- C) Stem-and-leaf plot
- D) Frequency distribution
- E) None of these

<u>Use the table to answer the following 2 questions</u>. Give your answer as a reduced fraction. The table shows the number of minority officers in a country's military in a certain year.

	Army	Navy	Marines	Air Force
African Americans	9162	3524	1341	4282
Hispanic Americans	2105	2732	914	1518
Other Minorities	4075	2653	599	3823

8. What is the probability that a randomly selected person is in the Marines?

(A) 1427/18364 (B) 1341/36728 (C) 3524/18309 (D) 1423/36728

**9.** Find the probability of selecting a person who is in the Navy, given that they are African American?

(A) 1427/18364 (B) 1341/36728 (C) None of these (D) 3524/18309 (E) 1423/36728

10. A bank offers a CD that pays a simple interest rate of 7%. How much must you put in this

CD now in order to have \$145.20 in 3 years?

a) \$120 b) \$141 c) \$127 d) \$123 e) None of these

- **11.** The price of a home is \$280,000. The bank requires a 15% down payment and two points at the time of closing. The cost of the home is financed with a 20-year fixed-rate mortgage at 6.5%. Find the amount of the mortgage.
- (A) \$42,000 (B) \$243,600 (C) None of these (D) \$261,900 (E) \$238,000

- **12.** A full-time employee who works 40 hours per week earns \$38,750 per year. Estimate that person's hourly income by rounding 52 weeks to 50 weeks per year, and round the annual income to the nearest thousand.
- a) \$19/hr b) \$19.50/hr c) \$19.38/hr d) \$20/hr e) None of these

**13.** In the following graph, what are the odd vertices?



**14.** A car rents for \$290 per week plus \$1.25 per mile. Find the rental cost for a two-week trip of 500 miles for a group of three people.

	(A)	\$862.50	(B) \$4485	(C) \$915	(D) None of these	(E) \$120
--	-----	----------	------------	-----------	-------------------	-----------

**15.** Most financial advisors recommend that you spend no more than 28% of your gross monthly income for your mortgage payment. Suppose that your gross annual income is \$46,800. What is the maximum amount you should spend each month on a mortgage payment?

	(A) \$2,808	(B)\$13,104	(C) None of these	(D)\$1,092	(E) \$1310.4
--	-------------	-------------	-------------------	------------	--------------

- **16.** Scores on the GRE (Graduate Record Examination) are normally distributed with a mean of 556 and a standard deviation of 147. Use the 68-95-99.7 Rule to find the percentage of people taking the test who score between 262 and 556.
- (A) 49.85% (B) 47.5% (C) None of these (D) 99.7% (E) 95%
- **17.** A game is played using one die. If the die is rolled and shows a 6, the player wins \$40. If the die shows any other number, the player wins nothing. If there is a \$8 fee to play the game, what is the expected gain/loss for a player?
- (A) -\$1.33 (B) None of these (C) \$1.33 (D) \$0.00 (E) \$3.00

**18.** A fair coin is tossed 3 times in succession. The set of equally likely outcomes is: {*HHH*, *HHT*, *HTH*, *THH*, *TTH*, *THT*, *HTT*, *TTT*} Find the probability of getting a tail on the second toss. (A) None of these (B)  $\frac{1}{2}$  (C)  $\frac{3}{8}$  (D)  $\frac{1}{8}$  (E)  $\frac{1}{4}$ 

14

Employee's Rates	Matching Rates Paid by the Employer	Self-Employed Rates
• 7.65% on first \$118,500 of income	<ul> <li>7.65% on first \$118,500 paid in wages</li> </ul>	<ul> <li>15.3% on first \$118,500 of net profits</li> </ul>
<ul> <li>1.45% of income in excess of \$118,500</li> </ul>	<ul> <li>1.45% of wages paid in excess of \$118,500</li> </ul>	• 2.9% of net profits in excess of \$118,500

**19.** Use the 2016 FICA tax rates in the table below to solve the problem.

If you are self-employed and earn \$126,500, what are your FICA taxes, rounded to the nearest dollar?

(A)\$4.661	(B) \$9.181	(C) \$18,363	(D)\$19.355	(E) None of these
(1) \$ 1,001	(D) \$ 7,101	(0) \$10,000	(D)#17,555	(L) None of these

20.A complete graph with 15 vertices has how many Hamilton circuits?

a) 15	b) 15!	c) 14	d) 14!	e) None of these
-------	--------	-------	--------	------------------

**21.** Find the <u>taxable income</u> for a taxpayer who earned wages of \$30,800, received \$2100 in interest from a savings account, and contributed \$3400 to a tax-deferred retirement plan. The taxpayer was entitled to a personal exemption of \$4050 and had deductions totaling \$7100.

(A) \$18,350 (B) None of these (C) \$25,150 (D) \$22,400 (E) \$	\$14,150
-----------------------------------------------------------------	----------

**22.** Use the complete weighted graph shown to find the weight of the following Hamilton circuit:



**23.** Use a table of z-scores and percentiles to find the percentage of data items in a normal distribution that lie between: z = 0.4 and z = 2.6

(A) 34.46%	(B) 33.99%	(C) 65.54%	(D)66.01%	(E) None of these
------------	------------	------------	-----------	-------------------

									-		
Score, x	1	2	3	4	5	6	7	8			
Frequency, f	2	4	6	6	6	6	2	3			
<b>24.</b> Find the median for the data items in the frequency distribution.											
(A) 5.5	(B)	4	(C)	) 4.5	1)	)5	(E	E) None	of these		
<b>25.</b> Find the mean for the data items in the frequency distribution. Round to the nearest tenth. A) 4.3 B) 4.5 C) 4.0 D) 1.0 E) None of these											
<ul><li>26. Find the value of the annuity to the nearest dollar.</li><li>Periodic Deposit: \$110 at the end of every six months</li><li>Rate: 4.5% compounded semiannually</li></ul>											
(A) \$3451 (	<b>me</b> : 20 years 3451 (B) \$2782 (C) N				ese	(D)\$7	7,016	(E) \$268			

Use the frequency distribution to answer the next 2 questions.

- 27. Does the graph have an Euler path, an Euler circuit, both, or neither?
  - A) The graph has an Euler path
  - B) The graph has an Euler circuit
  - C) The graph has both an Euler path **and** Euler circuit
  - D) The graph neither an Euler path nor an Euler circuit





- **29.** What is the value of an account with an initial balance of \$8500 after 5 years if it earns 7% interest compounded monthly? Round to the nearest cent.
- (A) None of these (B) \$11,921.69 (C) \$12,049.81 (D) \$10,419.10 (E) \$105,009.91



### Math 101 Final Exam Spring 2022

The theater society members are voting for the kind of play they will perform next semester: a comedy (C), a drama (D), or a musical (M). Their votes are summarized in the following preference table. Use it to answer the following 3 questions.

	Number of Votes		18	10	10	3	1	1					
			First Choice	М	С	D	С	D	М				
			Second Choice	С	Μ	С	D	М	D				
			Third Choice	D	D	М	М	С	С				
30.	Which typ	e of play is	s selected using the	e Plura	ality-	with-	elimi	natior	ı me	thod?			
(A)	Musical	(	(B) Comedy (C) Drama (D) None of these										
31.	How man	y members	s selected Drama as	s their	· first	choi	ce?						
(A)	10	(B) Non	e of these (	(C) 1			(D)1	3		(E) 11			
32.	Which typ	e of play w	vas a "majority win	iner"?									
(A)	Musical	(	B) Comedy	((	2) Dra	ama			(D) There isn't a				
									]	majority winner			
33.	A tree is												
	(A) Any co	onnected g	raph										
	(B) Any g	raph witho	out circuits										
	(C) Any co	onnected g	raph with no circu	its									
	(D) Any co	onnected g	raph with circuits										
	(E) None	of these											
34.	A set of da	ata items is	normally distribu	ted wi	ith a i	mean	n of 60	) and a	a sta	ndard deviation of 12.			
	Convert 1	5 to a z-sco	)re										
		-	$(\mathbf{D}) \circ 7 \mathbf{c}$	C) 10			<b>(D)</b>	10					
	(A)-3./3	)	(B) 3./5 (	<u>(</u> ) 12			(D)-	12		(E) None of these			
35.	You are d	lealt one o	card from a stand	ard 5	2-ca	rd de	eck. F	ind th	ne p	robability of being dealt			
a) 4	4/13	b) 2/13	c) 13/2	d) 3/4	4	e)	Non	e of tl	hese				

**36.**You borrow \$9000 from a friend and promise to pay back \$9315 in 1 year. What simple interest rate, to the nearest tenth of a percent will you pay?

(A) 3.5% (B) 35.0% (C) 1.0% (D) 0.35% (E) None of these

**37**. Suppose that a certain car has the following average operating and ownership costs.

Average Costs per Mile									
Operating	Ownership	Total							
\$0.24	\$0.72	\$0.96							

If you drive 20,000 miles per year, what is the total annual expense for this car?(A) \$14,400(B) \$24,000(C) \$19,200(D) \$18,750(E) None of these

### Use the following data set to answer the next 2 questions.

# 1, 1, 1, 4, 7, 7, 7

**38.**Find the standard deviation. Round to the nearest hundredth.

- A) 2.85
- B) 3.00
- C) 9.00
- D) 8.14
- E) None of these

**39.**Find the midrange.

(A) 1	(B)7	(C) 6	(D)4	(E) None of these
-------	------	-------	------	-------------------

**40.** Express the fraction  $\frac{5}{8}$  as a percent. Round to one decimal place. a) 80.0% b) 6.3% c) 62.5% d) 78.1% e) None of these The last page of this exam is the formula sheet and z-score table. You may tear that page out of the exam for your reference.

### You must use a pencil to fill in your scantron!

#### Final Exam Formula Sheet. FEEL FREE TO TEAR OFF THIS LAST DOUBLE SIDED PAGE

Standard Scores and Percentiles												
z-score	Percentile	z-score	Percentile	z-score	Percentile	z-score	Percentile					
- 3.5	0.02	- 1.0	15.87	0.0	50.00	1.1	86.43					
- 3.0	0.13	- 0.95	17.11	0.05	51.99	1.2	88.49					
- 2.9	0.19	- 0.90	18.41	0.10	53.98	1.3	90.32					
-2.8	0.26	- 0.85	19.77	0.15	55. <b>96</b>	1.4	91.92					
-2.7	0.35	- 0.80	21.19	0.20	57.93	1.5	93.32					
-2.6	0.47	- 0.75	22.66	0.25	59.87	1.6	94.52					
-2.5	0.62	- 0.70	24.20	0.30	61.79	1.7	95.54					
-2.4	0.82	- 0.65	25.78	0.35	63.68	1.8	96.41					
-2.3	1.07	- 0.60	27.43	0.40	65.54	1.9	97.13					
- 2.2	1.39	- 0.55	29.12	0.45	67.36	2.0	97.72					
-2.1	1.79	- 0.50	30.85	0.50	69.15	2.1	98.21					
-2.0	2.28	- 0.45	32.64	0.55	70.88	2.2	98.61					
- 1.9	2.87	- 0.40	34.46	0.60	72.57	2.3	98.93					
- 1.8	3.59	- 0.35	36.32	0.65	74.22	2.4	99.18					
- 1.7	4.46	- 0.30	38.21	0.70	75.80	2.5	99.38					
-1.6	5.48	- 0.25	40.13	0.75	77.34	2.6	99.53					
- 1.5	6.68	- 0.20	42.07	0.80	78.81	2.7	99.65					
-1.4	8.08	-0.15	44.04	0.85	80.23	2.8	99.74					
- 1.3	9.68	-0.10	46.02	0.90	81.59	2.9	99.81					
- 1.2	11.51	- 0.05	48.01	0.95	82.89	3.0	99.87					
- 1.1	13.57	0.0	50.00	1.0	84.13	3.5	99.98					

#### Example set of 52 poker playing cards

Suit	Ace	2	3	4	5	6	7	8	9	10	Jack	Queen	King
Clubs	÷.	2 * * :	* * * * ;	** * * *;	** * * * *;	\$* * * * * *;	2++ +++ + + <u>1</u>	*** *** ***;	·***	**** ****	12,	<mark>گھ</mark> ا	K RANK
Diamonds	€ ♦	₹ ◆ • ₹	* • • •	:◆ ◆ ◆ ◆;	₹ <b>◆</b> ◆ ◆ ◆;	€• • • • • •;					* <b>*</b>	° 🛃	* •
Hearts	٠,	₹ ♥ ▲ ±	₹ ¥ ¥ ▲ 2	** * • •;	₩ ¥ ¥ ▲ ▲?	\$ <b>*</b> * * * * *;					² <b>, 3</b> ,	12,	F
Spades	<b>ث</b> ا	² • • :	*	** * * *;	** * * * *:	** * * * * *;		1000 0000 0000 0000	*** ***	<sup>™</sup> . 	· .	° 🍂	Ĩ.

P = the principal amount invested or borrowed (present value)

A = accumulated amount (future value) r = the interest rate (as a decimal)

t = time (in years) n = number of compound periods per year

PMT = loan payment

# 1) Simple Interest:

Interest = Prt

2) <u>Future Value (with Simple Interest):</u>

$$A = P(1 + rt)$$
 or  $P = \frac{A}{(1+rt)}$ 

# 3) Compound Interest -finite # of compound peri

(Loan or Investment)

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$
 or  $P = \frac{A}{\left(1 + \frac{r}{n}\right)^{nt}}$ 

# 4) <u>Compound Interest -continous</u>

$$A = Pe^{rt}$$

 $e \approx 2.71828$  (but use e-button on calulator)

# 5) Savings Formula (Annuities)

P = deposit made at the end of each time period

$$A = \frac{P\left[\left(1 + \frac{r}{n}\right)^{nt} - 1\right]}{\left(\frac{r}{n}\right)}$$

6) Savings formula (Annuities)



# 7) <u>Loan Formula (Amortization Formula)</u>:

$$PMT = \frac{P\left(\frac{r}{n}\right)}{\left[1 - \left(1 + \frac{r}{n}\right)^{-nt}\right]}$$